

Seismic behavior of Horizontally Irregular Structures: Consequence of Relative Orientation of Accelerogram

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Abstract—The present study investigates regarding seismic response of plan and vertically asymmetric building structures. The geometric mean of the response spectra for two orthogonal horizontal components of motion, commonly used as the response variable in predictions of strong ground motion. Measurement of ground motion depends on the orientation of the sensors installed in the field which illustrates that ground-motion intensity could differ for the same actual ground motion on different oriented structure as respect to measured orientation. The drift is examined on models of single-storey structures having symmetric and asymmetric (torsional-stiff, torsional-flexible) layouts subjected to an ensemble of bi-directional near-fault strong ground motions with and without distinct velocity pulses over different orientation. The representative structure is analysed under all earthquakes rotated to different orientations (0° to 90°) at an interval of 15° under bi-directional excitations. The records are again applied on different type of structures which is adequately modelled using distributed plasticity approach to capture the bi-directional interactions.

Analyzed results demonstrates that torsional amplification factor which depicts the variation of peak response (A_{asym}/A_{sym}) for both 'flexible side' and 'stiff side' over different orientations in the range of 0° to 90° computed at an interval of 15° . That maximum normalized element displacement which may called torsional amplification factor are vary more or less 10%, 20% and 30% for e_r/D 0.06, 0.14 and 0.22 respectively for $T=0.2$ sec, 1sec and 3 sec; τ 0.5, 1 and 1.5 and e_{ro} 45° and 90° between minimum and maximum values over all orientation taken here. It implies the orientation should take into consideration Relative amplification in response are calculated by taking averages of all five event which reveals that critical orientation, θ_c may or may not follow systematic trend in the neighbourhood of θ_c ($\pm 45^\circ$).

Keywords: Bi-directional, asymmetry; seismic; strength dependent stiffness; design chart

1. INTRODUCTION

Ground motions are often scaled to certain convenient target spectra in the response assessment of structures. The geometric mean of the response spectra for two orthogonal horizontal components of motion, commonly used as the

response variable in predictions of strong ground motion, depends on the orientation of the sensors as installed in the field. This means that the measure of ground-motion intensity could differ for the same actual ground motion. This depends on sensor orientation.

Structures are often constrained to be horizontally irregular for architectural and functional reasons. The seismic vulnerability of these systems has been observed during past earthquakes [2], [4], [5], [6] and [15]. Numerous investigations (e.g., [3], [7], [9], [10] and [17]) have been carried out to achieve insight into the basic trend in both elastic and inelastic seismic behavior of symmetric and asymmetric systems. These studies, which use a parametrically defined equivalent single-storey model, are well-documented elsewhere [15], and generally employ a force-based design approach. In traditional approaches, the period of a structure is estimated and changes in its lateral strength (achieved by changing the strengths of components) are assumed to have a negligible effect on its stiffness and period (i.e., constant stiffness model). Two useful design philosophies are conceptualized that recognize the significance of strength dependent stiffness. In the post elastic range of shaking, during severe earthquake, the resulting resistive forces may be envisioned to pass through the center of strength (CV) of the system. If the CV is close to center of mass (CM), i.e., for a small value of strength eccentricity (e_v), only minor torque will be generated. In this circumstance, it has been shown [1], [14], based on plastic mechanism analyses of a number of systems, that displacement ductility demand may be minimized by minimizing the strength eccentricity, in the limit through 'CV-CM coinciding' design. On the other hand, it is proposed and verified elsewhere [11], [12], [13] and [18] that an efficient strength design strategy is to ensure a 'Balanced-CV-CR' criterion, i.e., strength should be distributed among the load-resisting elements so that the center of strength (CV) and center of resistance (CR) is located on either side of the center of mass (CM). However, the distance of CV and CR with respect to CM depends on the

performance states. Physically, such a strength design may tend to balance the elastic torque and plastic torque up to a given threshold. The state-of-the-art review also reveals that there is latitude to explore the seismic response of a plan asymmetric system by categorizing it into two classes depending upon the nature of prevailing stiffness eccentricity. Systems with eccentricity along one principal direction, parallel to any one side of the rigid deck, are designated as uni-directionally eccentric or mono-symmetric; whereas systems with eccentricities in two principal directions are referred to as bi-directionally eccentric [16].

Predictably, two translational components of a real accelerogram are applied along two principal axes of the structures conceited thereby that the orientation of the recording sensors are aligned with the principal axes of the structure. This may hardly represent the reality. Many studies in the past have recognized the strong dependency of the response on angle of incidence. Studies by [10] have confirmed that the identification of the angle leading to the worst inelastic response may not appear possible.

The authors, in this background, aim to examine the influence of angle of incidence on seismic demand of plan-asymmetric systems. Systems are idealized with equivalent single storey model, where load-resisting elements follow strength-dependent stiffness behaviour. The study appears to offer useful impression on the influence of angle of incidence in plan-asymmetric systems and hence may be important for practical purpose.

2. IDEALIZATION OF STRUCTURE AND METHODOLOGY

Structure have been idealized as rigid diaphragm model with three degrees of freedom at each floor level, two translations in two mutually orthogonal horizontal directions and one in-plane rotation. Masses are assumed to be lumped at the floor levels. The total storey stiffness can be evaluated from standard Eigen value problem knowing the lateral period and mass matrix of the system. Generally, in office buildings, lateral load-resisting structural members are found to be uniformly distributed over its plan. To represent such plan-wise distribution of the load-resisting elements (say, columns); in the present investigation, the structure is modeled to consist of six such elements, three in each orthogonal direction. The locations of the outer edge elements and subsequently the intermediate distance D may vary depending on the various characterizing parameters unlike several previous studies. Fifty per cent of the total lateral stiffness is attributed to the middle element and the rest 50% is equally distributed between two edge elements.

Standard system parameters such as mass, mass moment of inertia; stiffness, strength of the elements etc. are given as basic input to the program. The entire time domain is divided into a large number of time steps. In the parametric simulation, mass of the system is adjusted to achieve a target

lateral uncoupled period, while different torsional periods are set to regulate the distribution of the mass by varying the radius of gyration. A simple elasto-plastic hysteresis model is used as constitutive characteristics of the load-resisting elements. Under specified ground acceleration histories, standard equations of motion are solved in the time domain using Newmark's β - γ scheme, which considers constant average acceleration over each incremental time step. While Newmark's parameters γ and β are chosen, respectively, as 0.5 and 0.25, iterations are performed in each incremental time step using the modified Newton-Raphson technique. The time step of integration is taken as less than $T/1000$ second to ensure convergence (T is the lateral natural period of the system). 2% of critical damping in each mode of vibration is considered to constitute the damping matrix. The response of asymmetric structures normalized due to dynamically equivalent reference symmetric systems is presented to identify the impact of asymmetry alone. The normalization is done by dividing asymmetric system response by symmetric system response. Response are taken for every 15° interval from 0° to 90° because after 90° the values repeated itself in same presiding manner. Peak response under bi-directional excitation is marked.

Seismic response of structures is often evaluated by applying one (or two) horizontal component(s) of a recorded accelerogram along one (or two) principal axis(es) of the structure. This clearly ignores the possible influence of angle of incidence and should be prohibitive in practice. Ground motion components with reference to a new orientation defined by an angle ψ relative to the recorded component (refer to Fig. 2a) may be easily computed by the following simple transformation.

$$\begin{Bmatrix} a_{x(\psi)}(t) \\ a_{y(\psi)}(t) \end{Bmatrix} = \begin{bmatrix} \cos\psi & \sin\psi \\ -\sin\psi & \cos\psi \end{bmatrix} \begin{Bmatrix} a_x(t) \\ a_y(t) \end{Bmatrix} \quad (1)$$

in which $a_x(t)$, $a_y(t)$ are horizontal components of original record and $a_{x\psi}(t)$, $a_{y\psi}(t)$ the components of the record when rotated anti-clockwise by an angle ψ . We use 'orientation' (denoted by ψ) to refer to the issues related to ground motion alone, while 'angle of incidence' (denoted by θ) is used while response of structures is evaluated. Accelerogram at an angle of incidence θ with respect to principal axis of structure is equivalent to the accelerogram acting along the principal axis, but with orientation $\psi = \theta$ (illustrated in Fig. 2b). Thus to account for the different angles of incidences, ground motion components are rotated and applied along the principal axis of the structure.

3. RESULTS AND DISCUSSIONS

The response of systems with different orientation is computed under bi-directional ground motion applied along two principal directions of the system. Different eccentricities

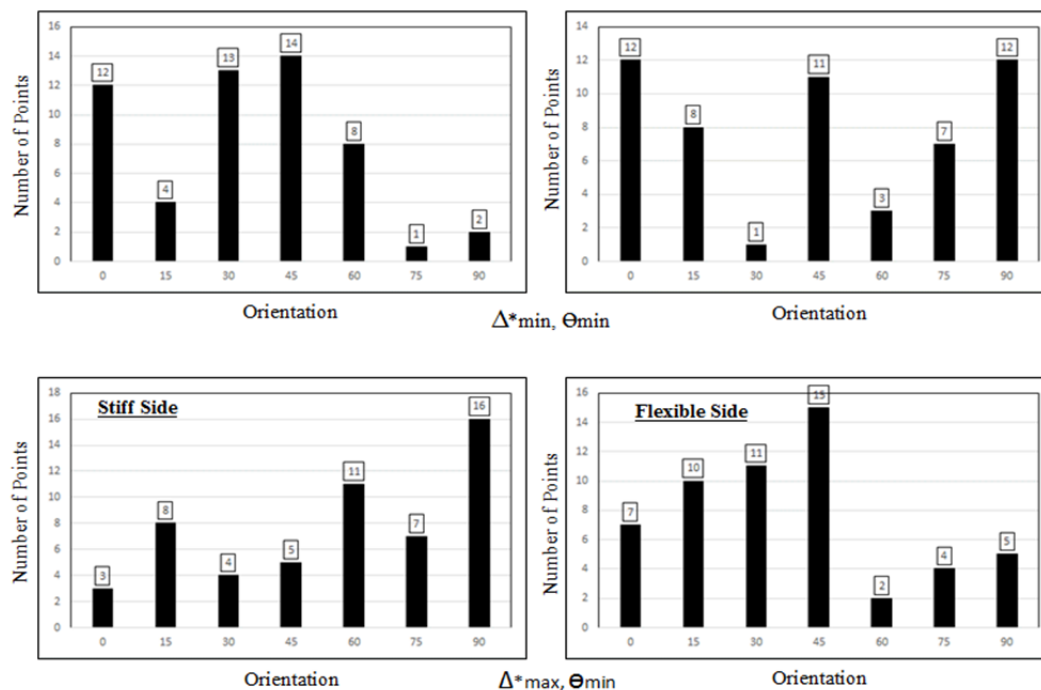


Figure 4: Summary of number of points in respective sides in different orientation at which maximum and minimum values of torsional amplification factor occurs.

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